

# Introduction to Biostatistics

## Exercises on Lecture 3

September 26, 2022

**(Q1):** The mean cholesterol levels for all 20-74 year old US males is  $\mu=211$  mg/100 ml and the corresponding sd is  $\sigma=46$  mg/100ml. If we selected repeated samples of size 25 from the population of 20-74 year old US males,

- What proportion of the samples will have a mean value of 200 mg/100ml or above?
- What proportion of the samples will have a mean value of 150 mg/100ml or below?

**(Q2):** What mean value of the serum cholesterol level cuts off the upper 10% of the sampling distribution of the sample means?

**(Q3):** What mean value of the serum cholesterol level cuts off the lower 10% of the sampling distribution of the sample means?

**(Q4):** What are the lower and upper mean values of the serum cholesterol level that enclose 95% of the sample means?

**(Q5):** There is an inverse relation between the level of confidence and the width of a CI. The more confidence we require, the less precise a statement we can make. How can we increase precision without loss of confidence, or vice versa?

**(Q6):** Which of the following are correct about a 95% CI

- There is a 95% chance that  $\mu$  is in the interval, i.e., the probability that  $\mu$  lies in  $\left(\bar{X} - 1.96 \frac{\sigma}{\sqrt{n}}, \bar{X} + 1.96 \frac{\sigma}{\sqrt{n}}\right) = 0.95$
- We are 95% confident that the interval contains  $\mu$ , i.e., the probability that the interval  $\left(\bar{X} - 1.96 \frac{\sigma}{\sqrt{n}}, \bar{X} + 1.96 \frac{\sigma}{\sqrt{n}}\right)$  contains  $\mu$  is 0.95